

# S+SSPR 2016

A Novel Graph Database for Handwritten Word Images &  
Graph-based Keyword Spotting in Historical Handwritten Documents

Plantation of Charles Sellars - the rest to Captain  
Locke's Company, at Nicholas Reasmers.  
October 26. G.W.

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th 3. Winchester: October 28<sup>th</sup> 1755.  
Parole Hampton.  
The officers who came down  
from Fort Cumberland with Colonel  
Washington, are immediately to go Recui-

## Team

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## Content

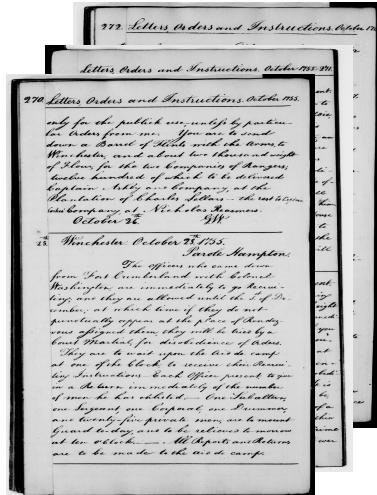
- Overview
- From Documents to Graphs
  - Image Preprocessing
  - Graph Representation
  - Graph Normalisation
  - Graph Matching
- Experiments
- Future Work
- Q+A

## Overview – What is Keyword Spotting

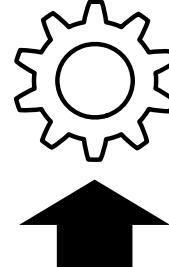
Keyword Spotting (KWS) is the task of **retrieving any instance** of a given **query** word in **speech recordings or text images**.

Focus on handwritten, historical documents

Document

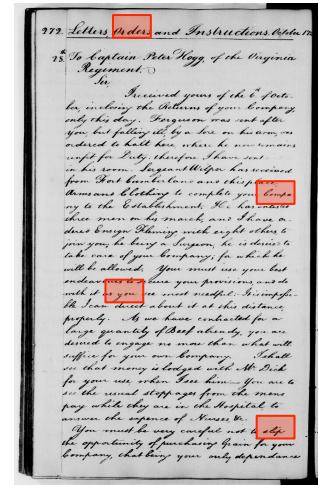
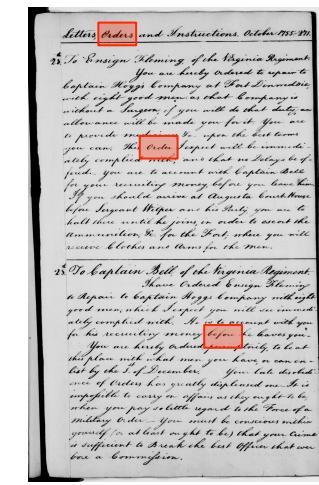
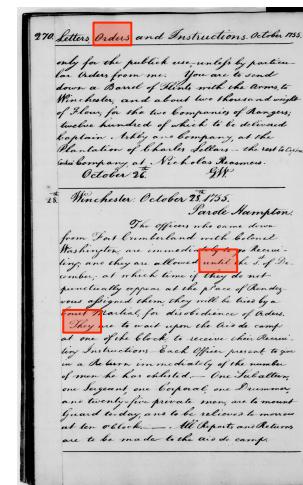


Query



Orders

Word Spotting

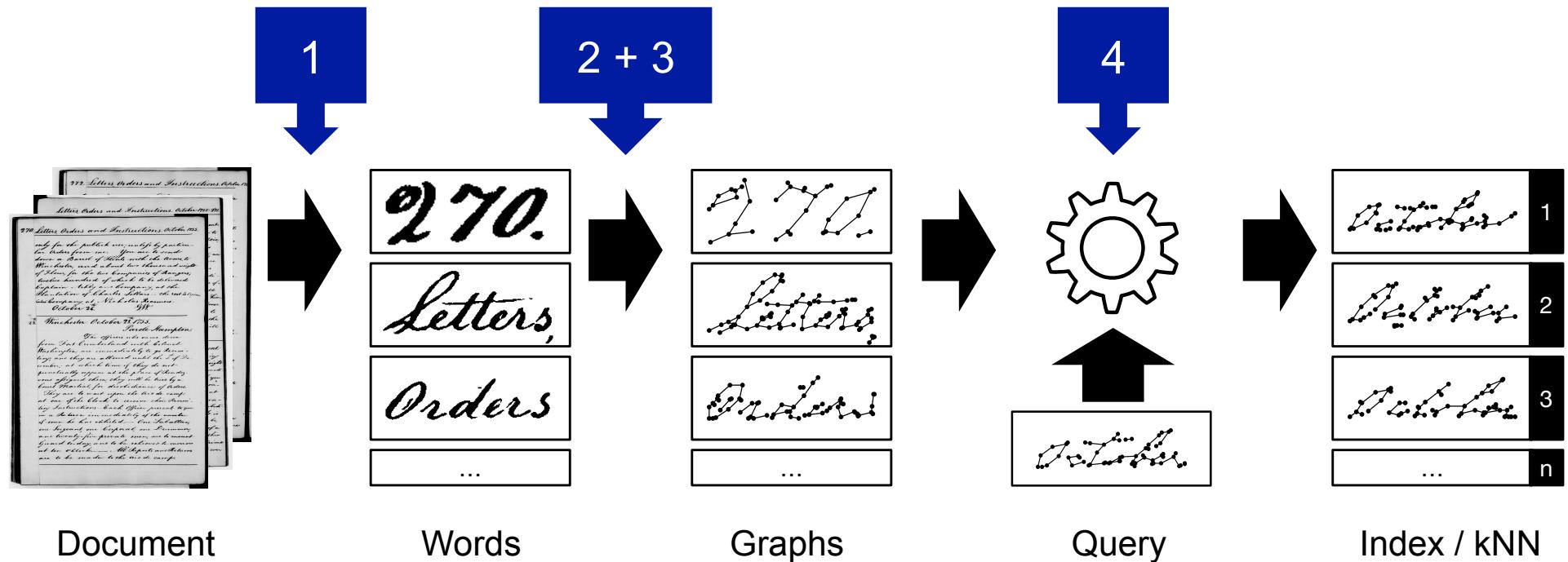


## Overview – From Documents to Graphs

### Process Legend

- 1) Image Preprocessing
- 2) Graph Extraction
- 3) Graph Normalisation
- 4) Pairwise Matching

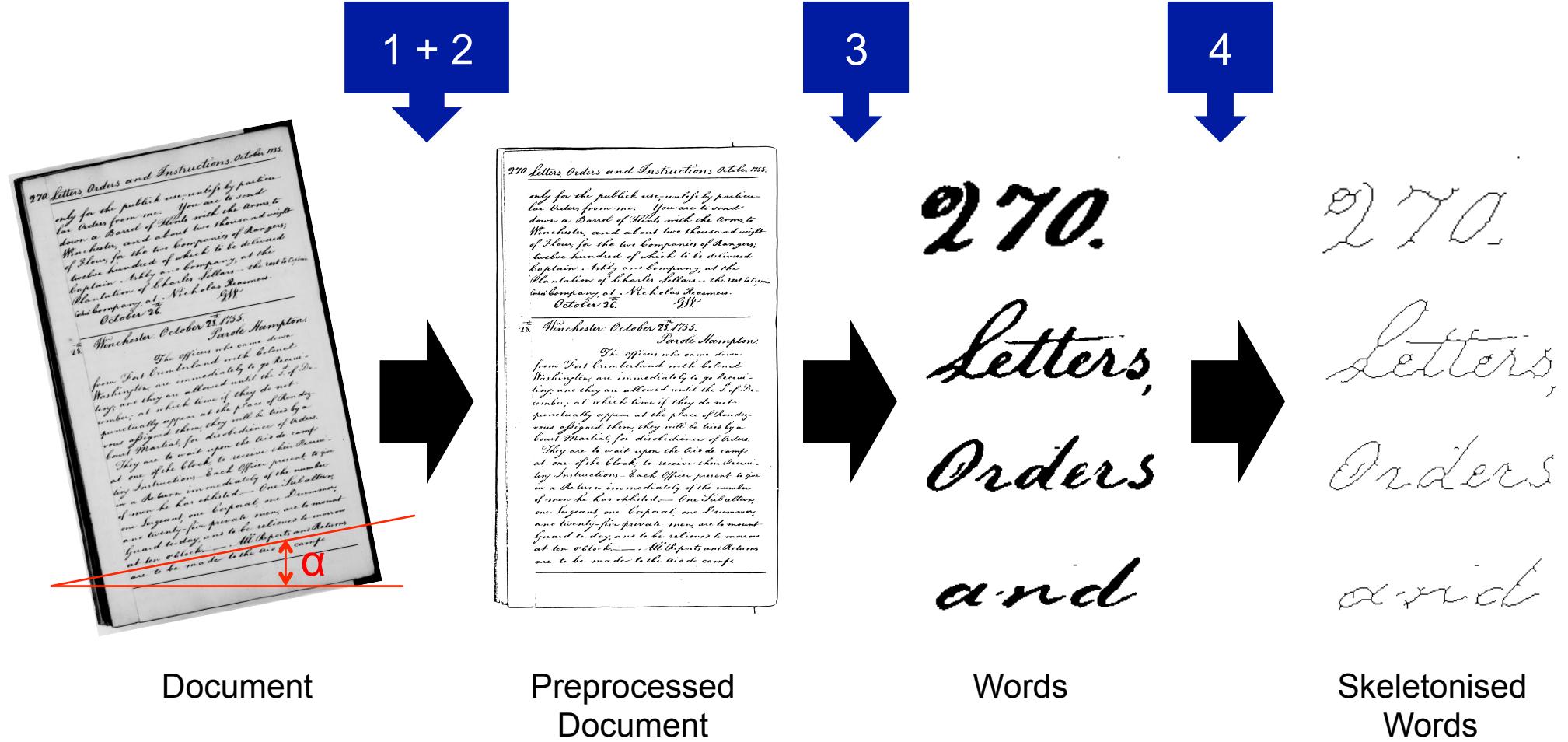
Graph-based KWS is based on the **representation of words** by means of different **graphs**. These representations are eventually used to **match a query graph against all document graphs**.



## 1) Image Preprocessing

### Process Legend

- 1) Binarisation / Difference of Gaussian
- 2) Skew Correction ( $\alpha$ )
- 3) Word Segmentation
- 4) Skeletonisation (optional)



## 2) Graph Extraction – Overview

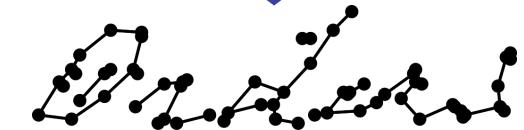
**Node Extraction**  
+  
**Edge Extraction**

- Keypoint** 1 + 2
  - Skeleton
- Grid** 1
  - Neighbourhood (NNA)
  - Minimal Spanning Tree (MST)
  - Delaunay (DEL)
- Projection** 1
  - Skeleton
- Split** 1
  - Skeleton

### Papers

- 1) A Novel Graph Database for Handwritten Word Images
- 2) Graph-based Keyword Spotting in Historical Handwritten Documents

*Orders*

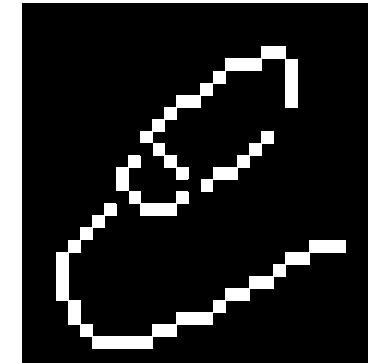


## 2) Graph Extraction – Keypoint (Node Extraction)

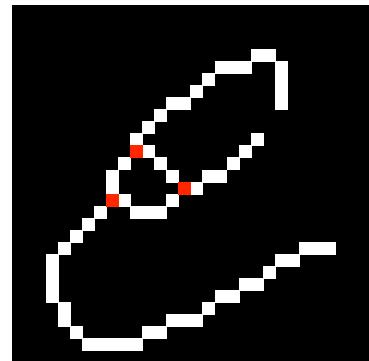
1) For each connected component...



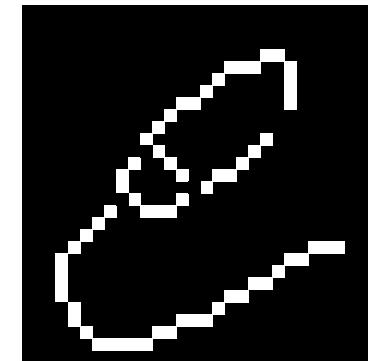
3) ...invert junction points



2) ...find junction points

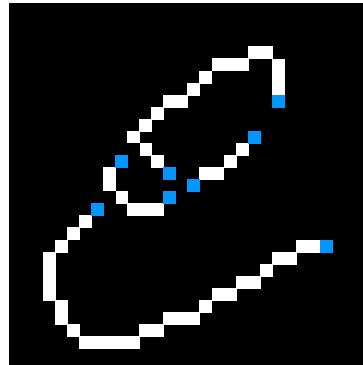


4) For each connected subcomponent...

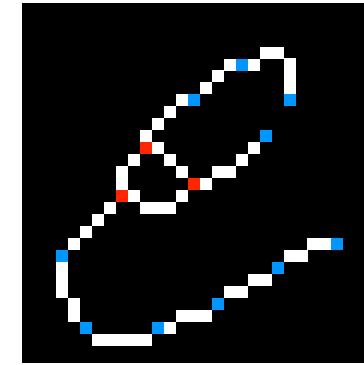


## 2) Graph Extraction – Keypoint (Node / Edge Extraction)

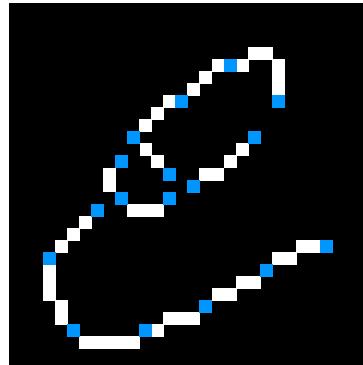
5) ...find start- and end points



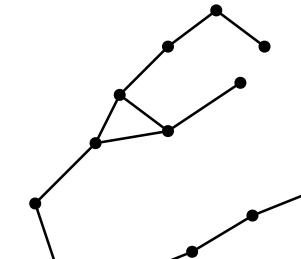
7) Replace neighbours of junction point

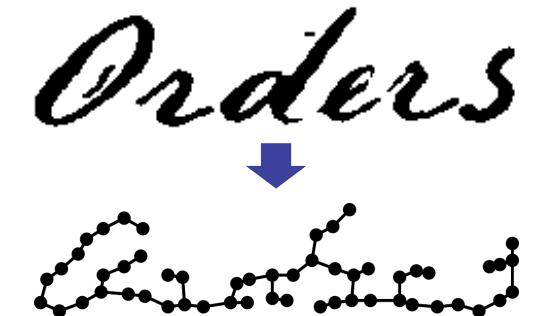


6) ...add nodes along path



8) Add edges based on skeleton



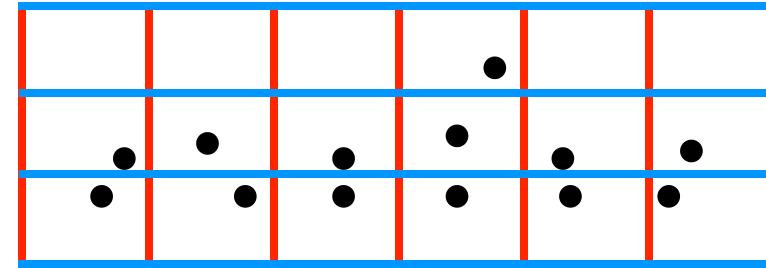


## 2) Graph Extraction – Grid (Node / Edge Extraction)

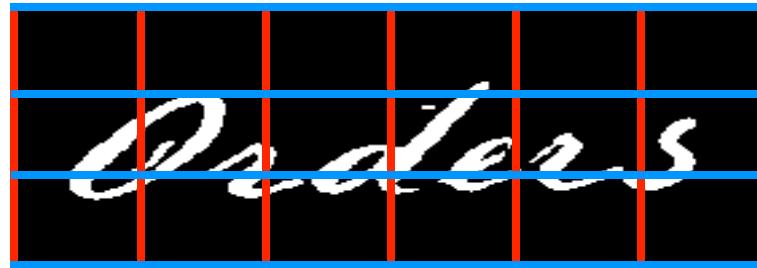
1) Add columns based on threshold



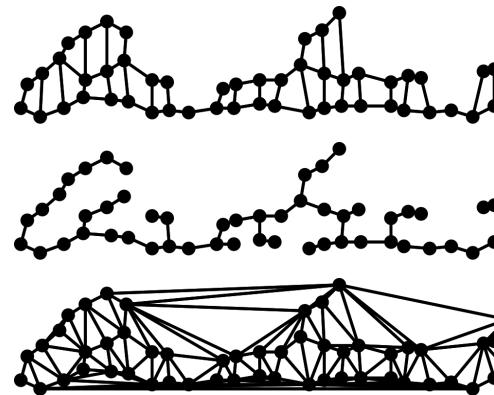
3) Add nodes based on centre of mass



2) Add rows based on threshold



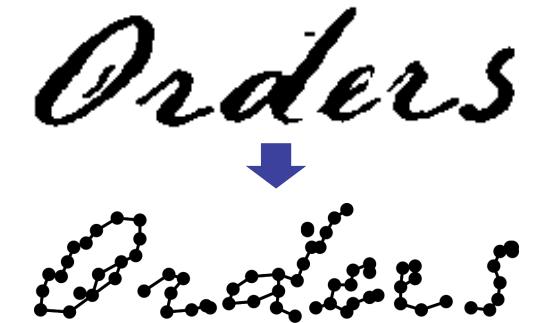
4) Add edges based on edge extraction



Neighbourhood  
Analysis (NNA)

Minimal Spanning  
Tree (MST)

Delaunay Tri-  
angulation (DEL)

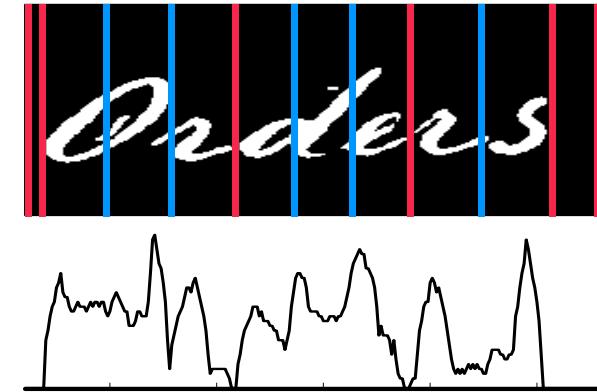


## 2) Graph Extraction – Projection (Node Extraction)

1) Vertical projection



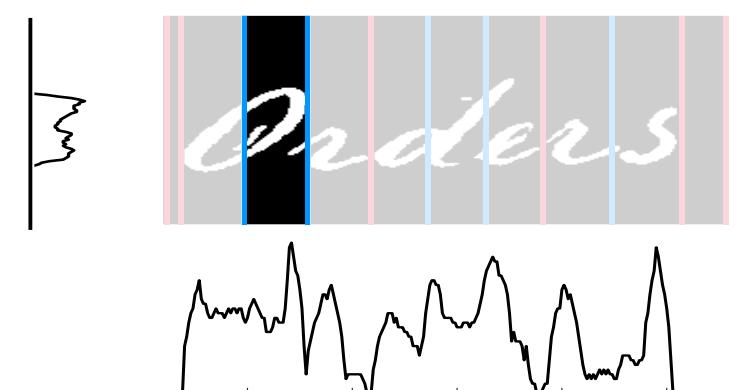
3) Add further columns based on threshold

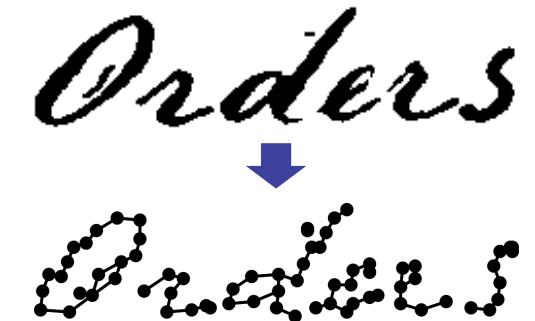


2) Add "null" positions as columns



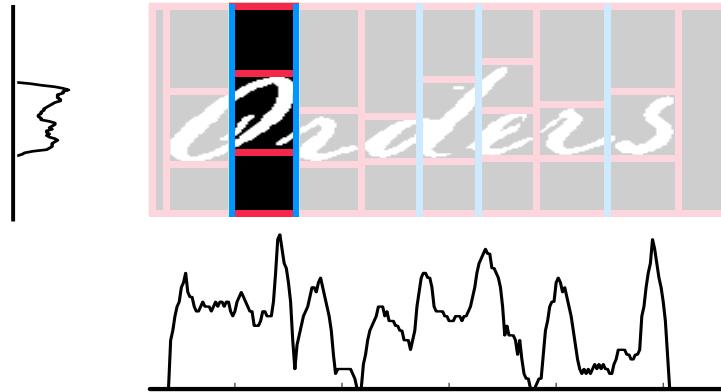
4) Horizontal projection per column



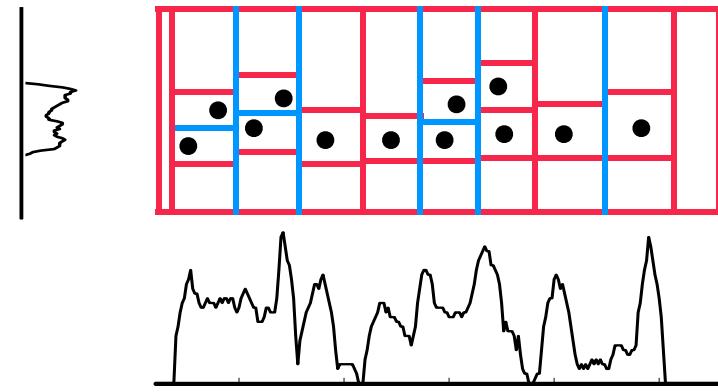


## 2) Graph Extraction – Projection (Node / Edge Extraction)

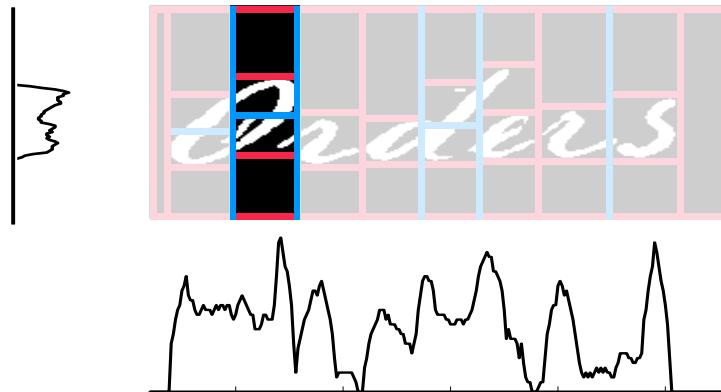
5) Add "null" positions as rows



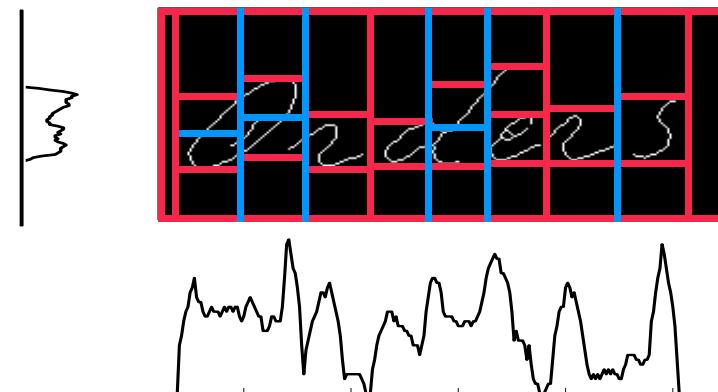
7) Add nodes based on centre of mass



6) Add further rows based on threshold



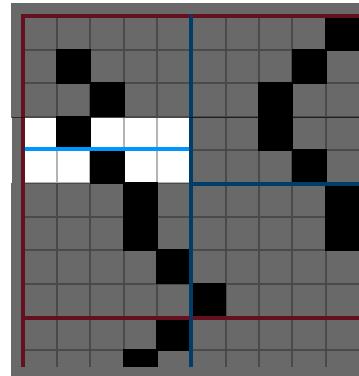
8) Add edges based on skeleton...



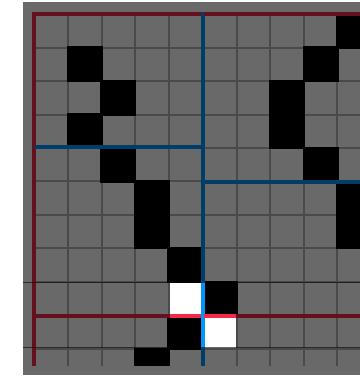


## 2) Graph Extraction – Projection (Edge Extraction)

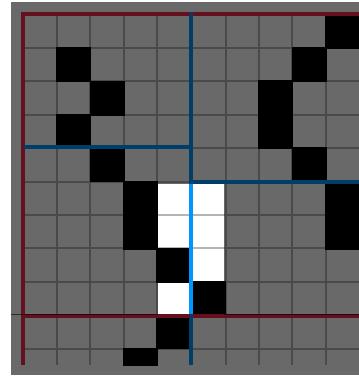
9) ...vertical



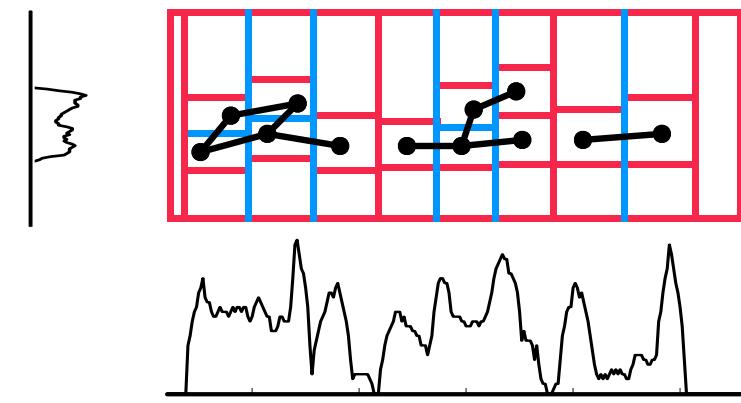
11) ...diagonal

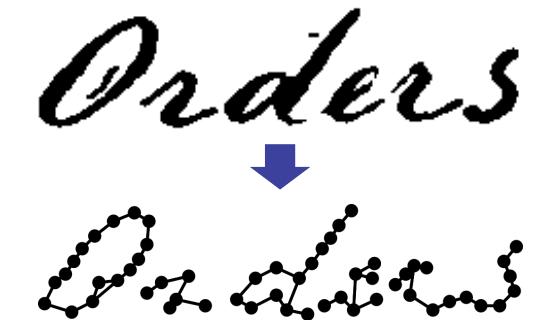


10) ...horizontal



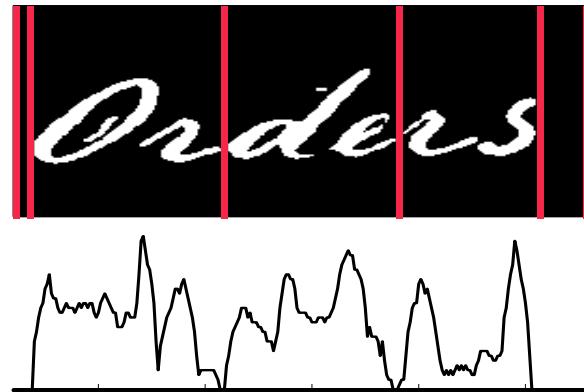
12) Complete graph





## 2) Graph Extraction – Split (Node Extraction)

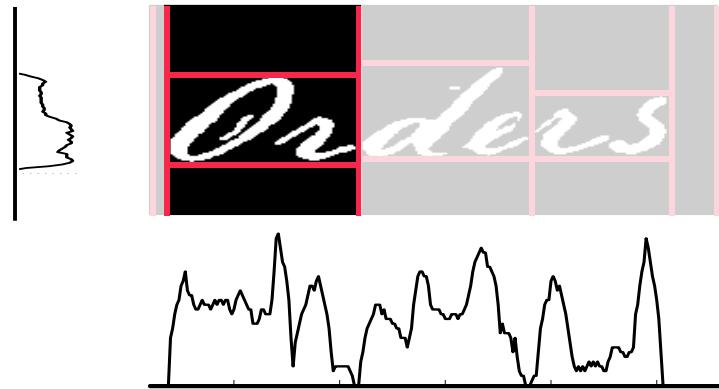
1) Split horizontal on null positions



3) For each subimage...

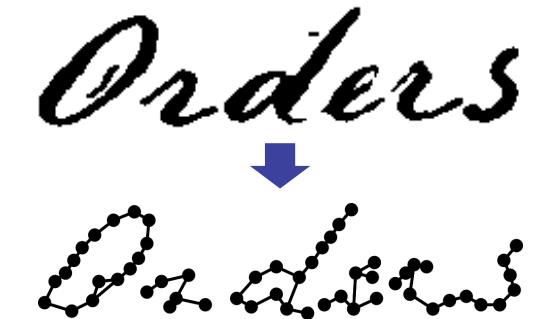


2) Split vertical on null positions



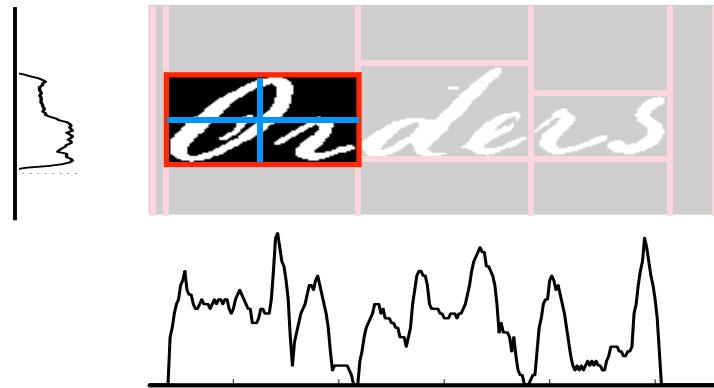
4) ...too wide? Split horizontal



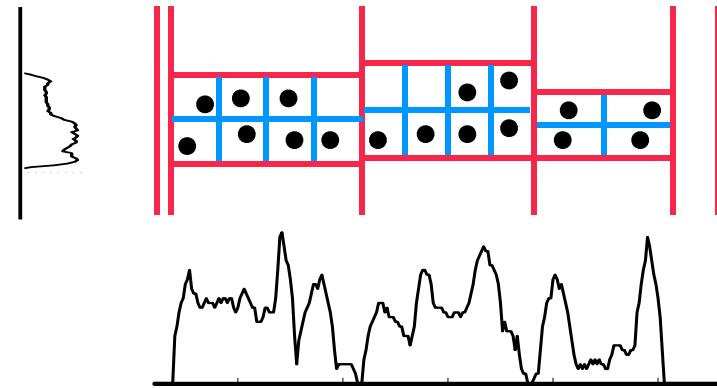


## 2) Graph Extraction – Split (Node / Edge Extraction)

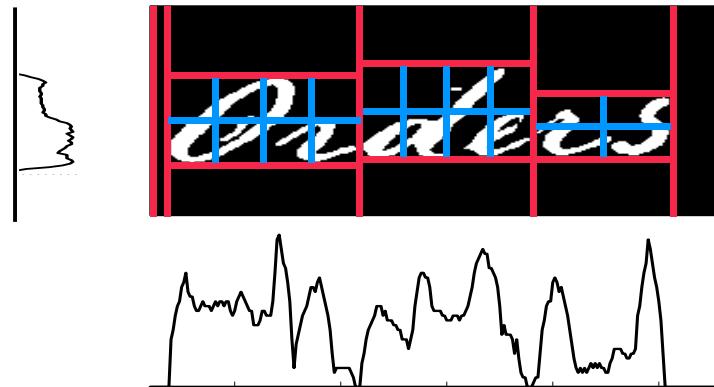
5) ...too high? Split vertical



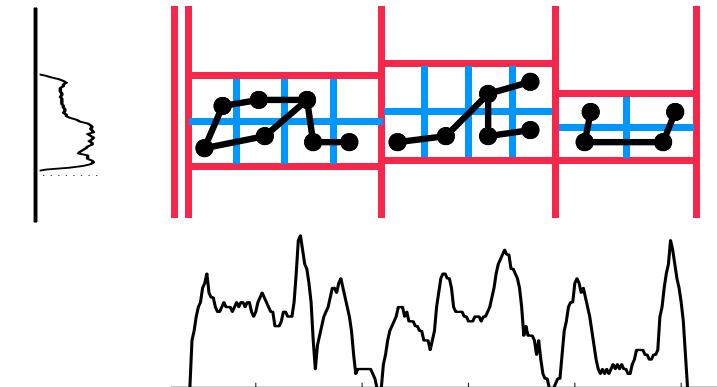
7) Add nodes based on centre of mass



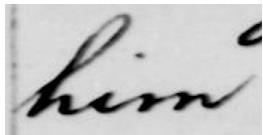
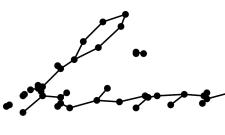
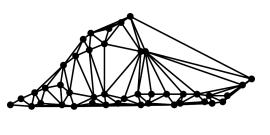
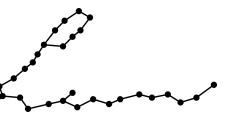
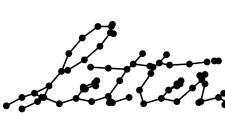
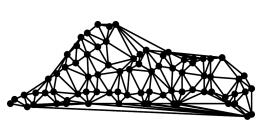
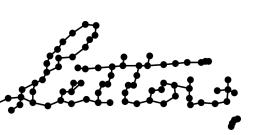
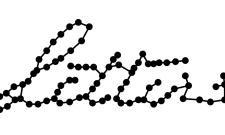
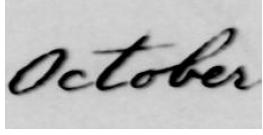
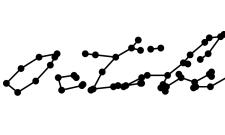
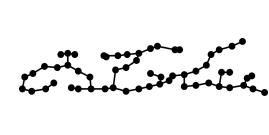
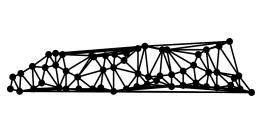
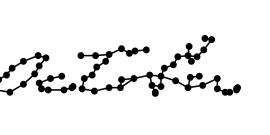
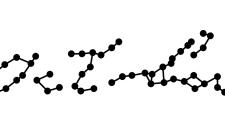
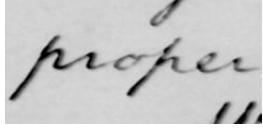
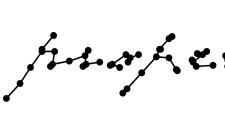
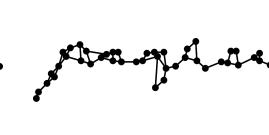
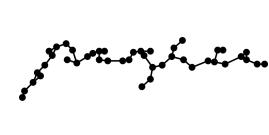
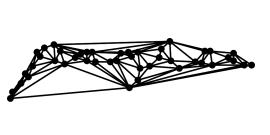
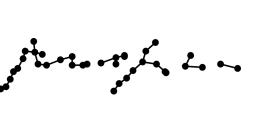
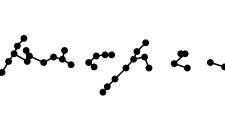
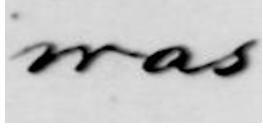
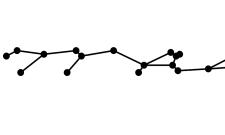
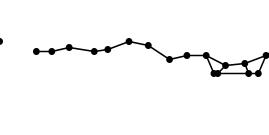
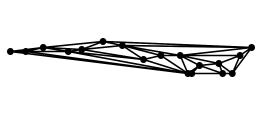
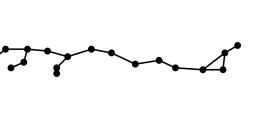
6) Split until subimages < threshold



8) Add edges based on skeleton



## 2) Graph Extraction – Resulting Graphs

Word Image	Keypoint	Grid-NNA	Grid-MST	Grid-DEL	Projection	Split
						
						
						
						
						

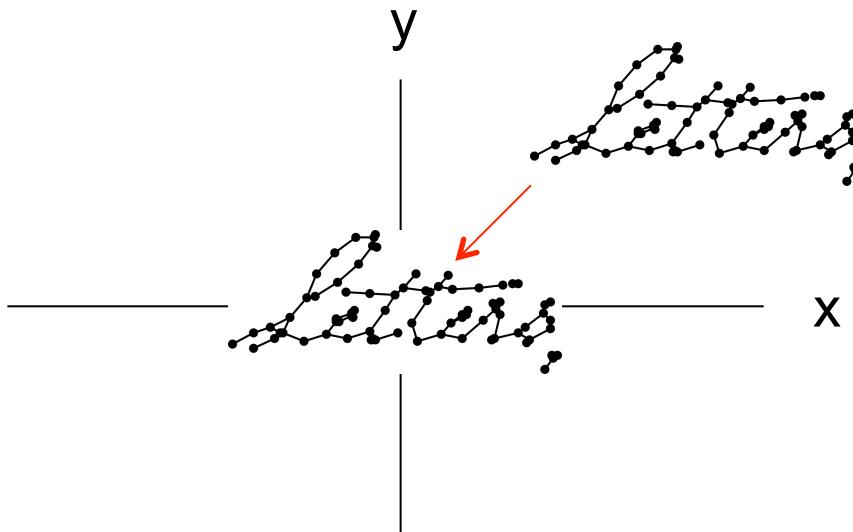
### 3) Graph Normalisation – Size & Position of Nodes

#### Centering

$$x_n = x - \mu_x$$

$$y_n = y - \mu_y$$

$\mu$  is mean of node positions

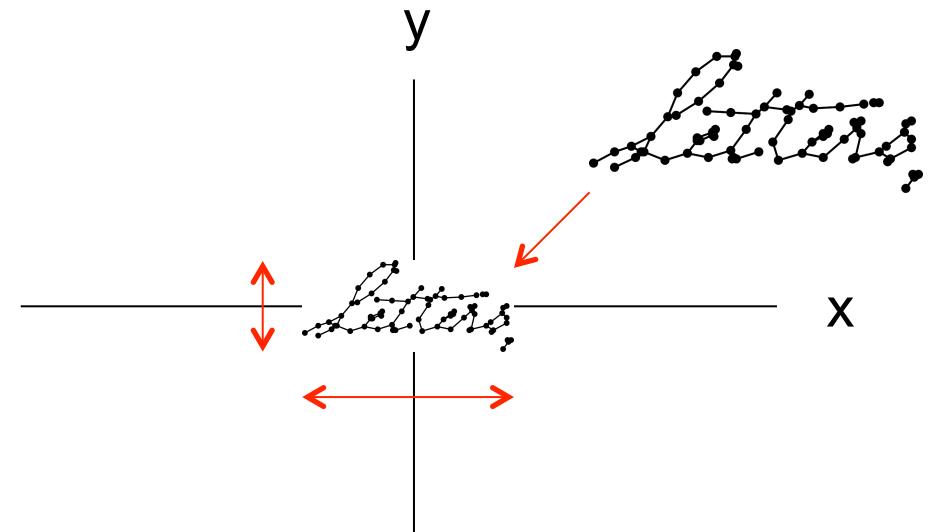


#### Centering & Scaling

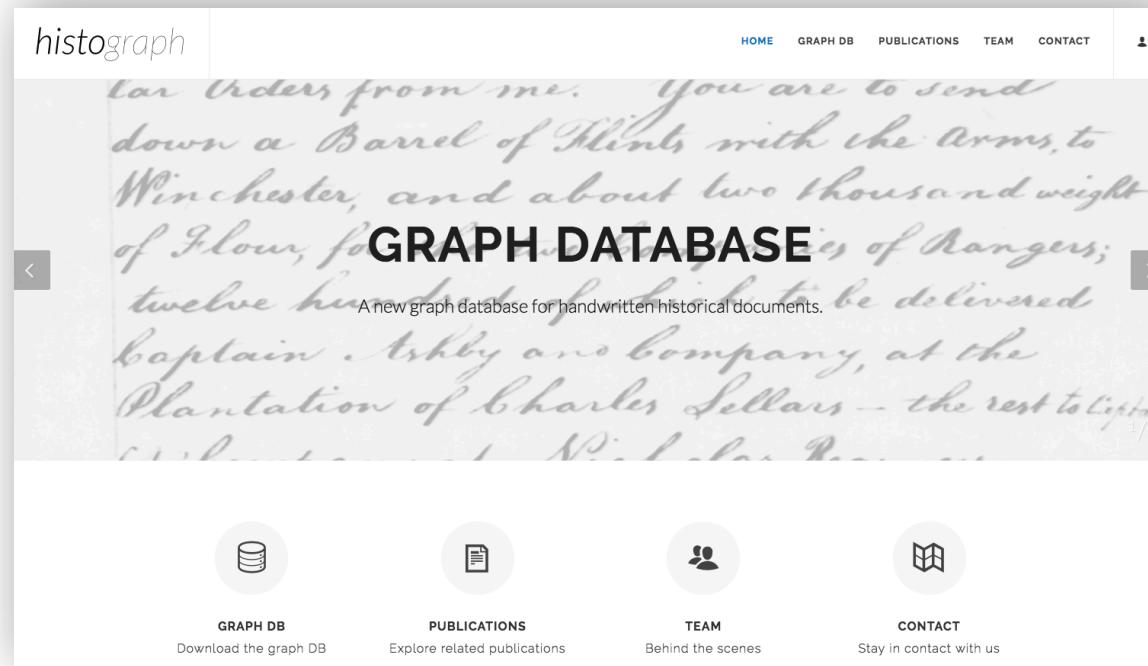
$$x_n = (x - \mu_x) / \sigma_x$$

$$y_n = (y - \mu_y) / \sigma_y$$

$\sigma$  is standard deviation of node positions



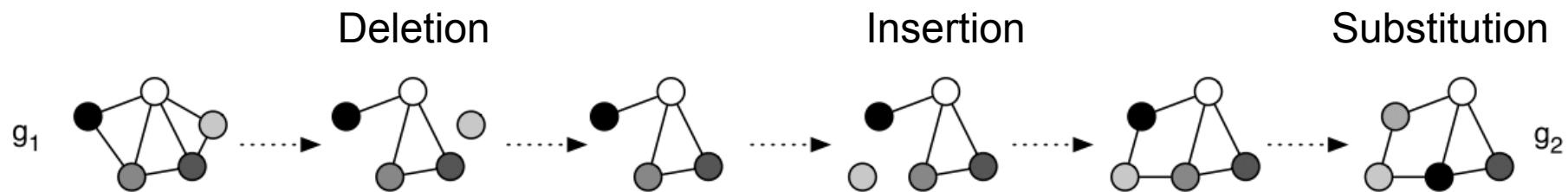
### 3) Graph Normalisation – Graph DB



All graphs are available at **histograph.ch**

## 4) Graph Matching – Graph Edit Distance

Graph Edit Distance (GED) measures the **minimum amount of distortion** that is needed to **transform one graph into another**.

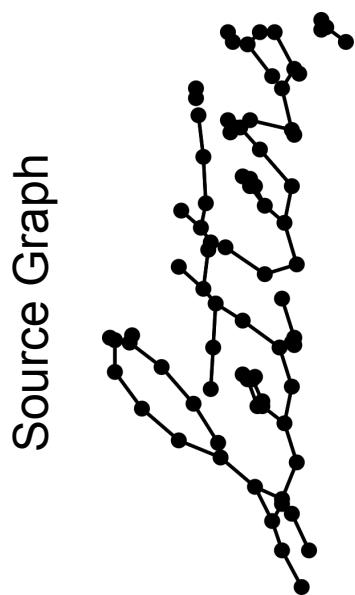


Exact GED is exponential in the number of nodes of the involved graphs and therefore intractable.



We make use of approximated GED

## 4) Graph Matching – Bipartite Graph Matching



Target Graph				
$\begin{bmatrix} c_{11} & c_{12} & \cdots & c_{1m} & \\ c_{21} & \text{Substitution Costs} & c_{2m} \\ \vdots & & \vdots \\ c_{n1} & c_{n2} & \cdots & c_{nm} & \\ \hline c_{\varepsilon 1} & \infty & \cdots & \infty & \\ \infty & \text{Insertion Costs} & \vdots \\ \vdots & & & \infty \\ \infty & \cdots & \infty & c_{\varepsilon m} & \end{bmatrix}$				
Cost Matrix with Node Edit Costs				

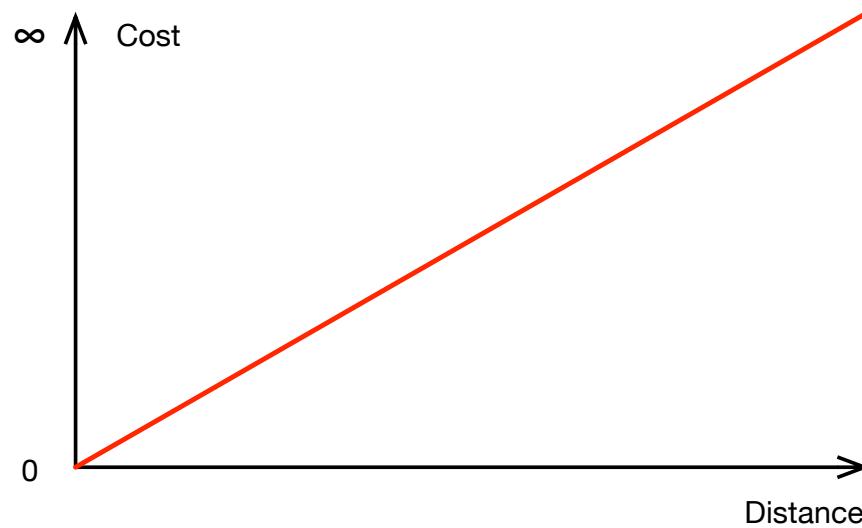


Approximative GED  
via Linear Sum  
Assignment Problem

## 4) Graph Matching – Substitution Cost Functions

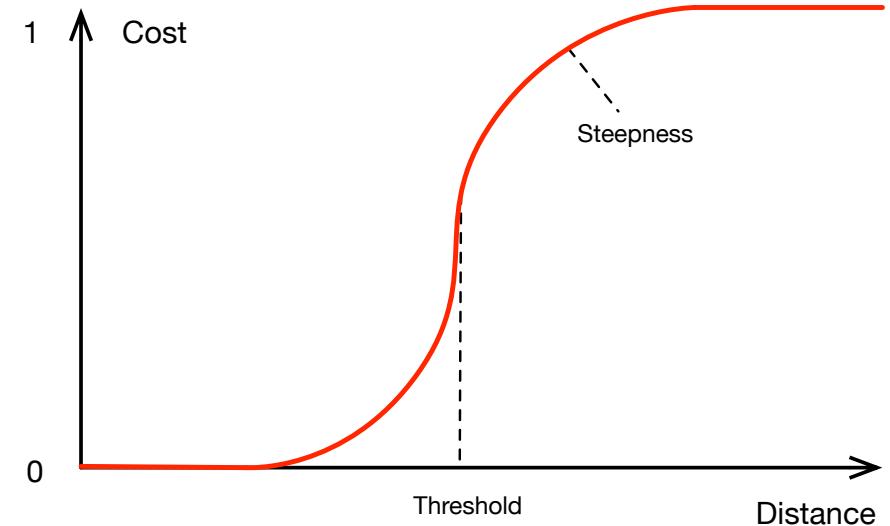
**Euclidean**  $c_{\text{Euclidean}}$

$$c_E(u \rightarrow v) = \sqrt{\alpha(x_i - x_j)^2 + (1 - \alpha)(y_i - y_j)^2},$$



**Sigmoidal**  $c_{\text{Sigmoidal}}$

$$c_S(u \rightarrow v) = \frac{2\tau_v}{1 + e^{(kc_E(u \rightarrow v) - \gamma)}}$$



For deletion and insertion of nodes and edges we assume fixed costs

## Abbreviations

$|V|$  Median number of nodes  
 $|E|$  Median number of edges

## Experiments – Setup / Results Graph DB (kNN)

<b>Set</b>	Instances per Word Class	<b>Size</b>
Training	3	90
Validation	2	60
Test	3 - 5	143

<b>Graph Extraction Algorithm</b>	$ V $	$ E $	<b>Accuracy</b>
Keypoint	73	67	0.7762
Grid-NNA	39	55	0.6502
Grid-MST	46	44	0.7413
Grid-DEL	52	138	0.6294
Projection	44	41	0.8182
Split	51	48	0.8042

## Experiments – Setup KWS

Set	Instances per Word Class	Size
Training	> 10	1000
Validation	1	10
Training	> 1	1223.5 (avg)
Test	> 1	2447.0 (avg)

→ Quality is measured by the **mean Average Precision (mAP)**

Recall = True Positives / (True Positives + False Negatives)

Precision = True Positives / (True Positives + False Positives)

mAP = Average area under the curve of Precision-Recall curves

## Abbreviations

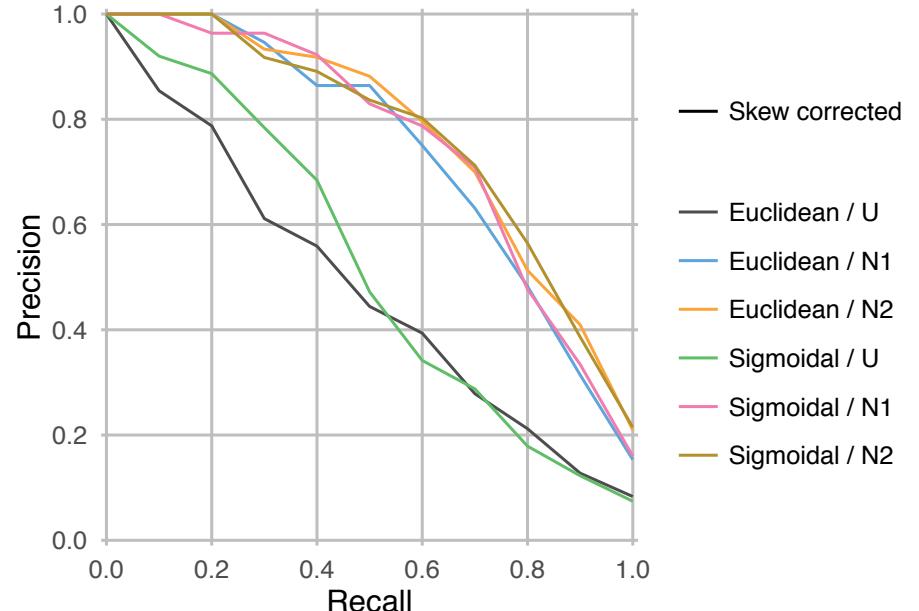
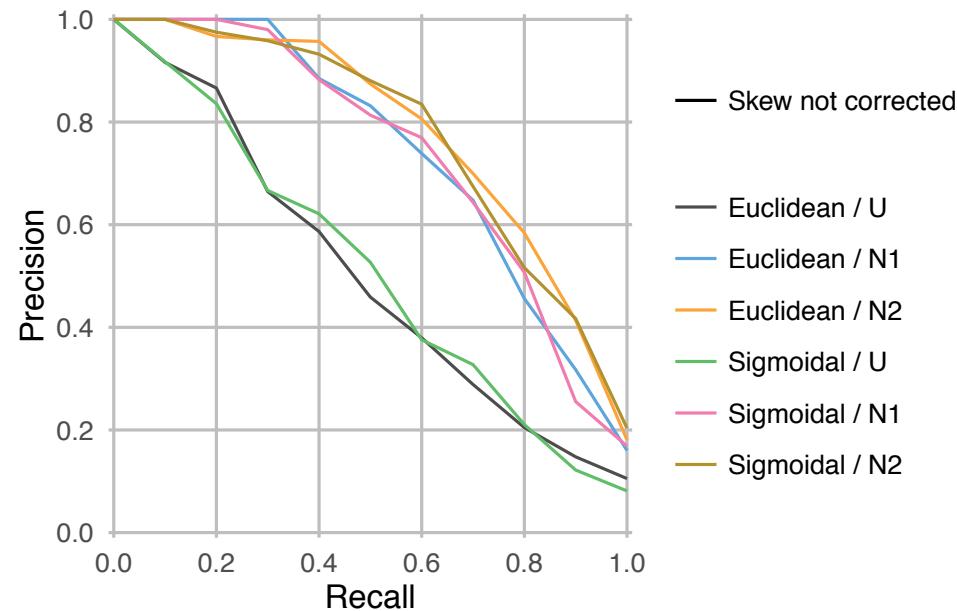
U Not normalised

$N_1$  Centering

$N_2$  Centering + Scaling

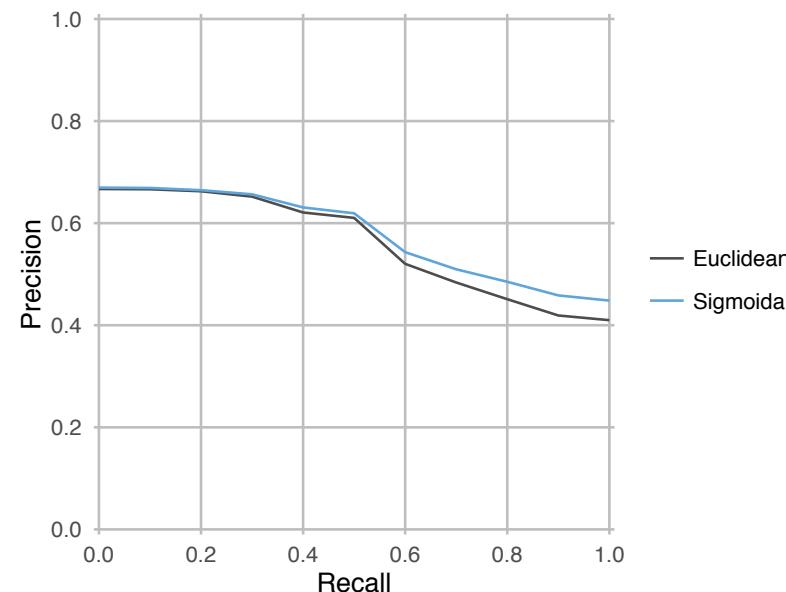
## Experiments – Results KWS (mAP) / Validation

Preprocessing	Skew not corrected			Skew corrected		
Cost Function	U	$N_1$	$N_2$	U	$N_1$	$N_2$
$C_{\text{Euclidean}}$	50.17	72.87	<b>76.53</b>	47.08	72.24	75.59
$C_{\text{Sigmoidal}}$	49.71	72.72	<b>76.24</b>	50.60	73.53	75.24



## Experiments – Results KWS (mAP) / Testing

System	mAP	Improvement
Dynamic Time Warping (DTW)	54.08	
Proposed $c_{\text{Euclidean}}$	55.33	+ 2.31 %
Proposed $c_{\text{Sigmoidal}}$	57.12	+ 5.62 %



## Future Work

### Database Extension

- Further documents (e.g. Parzival dataset)

### Graph Representation

- Further node and edge labels

### Graph Matching

- Speeding up graph matching procedure

### Experiments

- Evaluate all graph extraction methods with KWS experiment

Q+A

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